

# Introducing Connection Minimal Abduction for $\mathcal{EL}$ Ontologies <sup>\*</sup>

Fajar Haifani<sup>1</sup> , Patrick Koopmann<sup>2</sup> , and Sophie Tournet<sup>1,3</sup> 

<sup>1</sup> Max Planck Institute for Informatics, Saarland Informatics Campus, Saarbrücken  
Germany (`{fhaifani,stourret}@mpi-inf.mpg.de`)

<sup>2</sup> Institute for Theoretical Computer Science, Technische Universität Dresden,  
Germany (`patrick.koopmann@tu-dresden.de`)

<sup>3</sup> Université de Lorraine, CNRS, Inria, LORIA, Nancy, France

**Abstract.** We introduce a new, explanation-oriented, minimality notion for abduction in the description logic  $\mathcal{EL}$ . It rejects solutions where a random concept inclusion, disconnected from the problem at hand, is used.

**Keywords:** Abduction · Description Logic  $\mathcal{EL}$  · Minimality Criterion.

## 1 Introduction

Ontologies are used in many areas to represent and reason about terminological knowledge. Usually, they consist of a set of axioms formulated in a description logic (DL), giving definitions of concepts, or stating relations between them. Especially in the bio-medical domain, we often find ontologies that contain a lot of those axioms, for instance, SNOMED CT<sup>4</sup> containing over 350,000 axioms, or the Gene Ontology GO<sup>5</sup> defining over 50,000 concepts. A central reasoning task for ontologies is to determine whether one concept is subsumed by another, a question that nowadays can be answered rather efficiently using highly optimized description logic reasoners [23]. If the answer to this question is unexpected or hints at an error, a natural interest is in an explanation for that answer—especially if the ontology is complex. Such an explanation can help in understanding the internal mechanisms of an ontology, as well as facilitate debugging. Explaining positive entailments—e.g., explaining why a concept subsumption holds—is well-researched in the DL lecture, and typical approaches use justifications [5, 17, 26] or proofs [1, 2], functionalities that are integrated into standard ontology editors [18, 19]. The problem of explaining negative entailments—e.g. explaining why a subsumption does not hold—is less investigated, and there is no standard tool support. Classical approaches involve providing a counter-example [6], or using *abduction*.

---

<sup>\*</sup> Funded by DFG grant 389792660 as part of TRR 248 – CPEC, see <https://perspicuous-computing.science>)

<sup>4</sup> <https://www.snomed.org/>

<sup>5</sup> <http://geneontology.org/>

In abduction, a missing entailment  $\mathcal{T} \not\models \alpha$  is explained by providing a “missing piece”, the *hypothesis*, that, when added to the ontology, would entail the answer. It can thus be used to explain why the entailment does not hold, and even provide for a possible fix in case the entailment should hold. In the DL context, depending on the shape of the (missing) observation to be explained, one distinguishes between concept abduction [7], ABox abduction [8–11, 14, 16, 20, 21, 24, 25], TBox abduction [12, 27] or knowledge base abduction [15, 22]. We are here focussing on TBox abduction, where we assume that ontology, observation and hypothesis consist only of TBox axioms.

Commonly, to avoid trivial answers, the user provides syntactic restrictions on hypotheses, such as a set of abducible axioms to pick from [9, 24], a set of abducible predicates [21, 22], or even patterns on the shape of the answer [13]. But even with those restrictions in place, there may be many possible solutions to an abduction problem, and the question is how to find the ones with the best explanatory potential. It is here common to either provide a representation that covers all explanations at the same time [22], or to apply minimality criteria such as subset minimality, size minimality, or semantic minimality [8] to prune the set of solutions. We argue that using those more superficial minimality criteria may still lead to hypotheses that are not that helpful, as they ignore the deeper logical structure of the hypotheses and their connection to the observation. To address this issue, we introduce a new minimality criterion called *connection minimality*, which we define for the lightweight description logic  $\mathcal{EL}$ .

## 2 Preliminaries

We recall the description logic  $\mathcal{EL}$  and provide a formal definition of the abduction problem as used in this abstract.

Let  $\mathbf{N}_C$  and  $\mathbf{N}_R$  be pair-wise disjoint, countably infinite sets of respectively *atomic concepts* and *roles*. Generally, we use letters  $A, B, E, F\dots$  for atomic concepts, and  $r$  for roles, possibly annotated. Letters  $C, D$ , possibly annotated, denote  $\mathcal{EL}$  *concepts*, built according to the syntax rule  $C ::= \top \mid A \mid C \sqcap C \mid \exists r.C$ . We assume that conjunctions are treated as sets, that is, we ignore nested conjunctions, and assume that the order of conjuncts is not important. For a set  $N$  of concepts, we denote by  $\prod N$  the conjunction over all elements in  $N$ . An  $\mathcal{EL}$  *TBox*  $\mathcal{T}$  is a finite set of *concept inclusions* of the form  $C \sqsubseteq D$ . We use  $C \equiv D$  as abbreviation for  $C \sqsubseteq D, D \sqsubseteq C$ . The semantics of  $\mathcal{EL}$  is defined as usual (see e.g. [3]). Specifically, for a TBox  $\mathcal{T}$ , we use  $\mathcal{T} \models C \sqsubseteq D$  to denote that  $C \sqsubseteq D$  holds in all models of  $\mathcal{T}$ , in which case we also say  $C \sqsubseteq D$  is *entailed* by  $\mathcal{T}$ .

**Definition 1.** *Given a TBox  $\mathcal{T}$ , a set of atomic concepts  $\Sigma \subseteq \mathbf{N}_C$  and a concept inclusion  $C_1 \sqsubseteq C_2$ , denoted as the observation, where  $C_1$  and  $C_2$  are atomic concepts and  $\mathcal{T} \not\models C_1 \sqsubseteq C_2$ , the corresponding TBox abduction problem, denoted as the tuple  $\langle \mathcal{T}, \Sigma, C_1 \sqsubseteq C_2 \rangle$ , is to find a TBox*

$$\mathcal{H} \subseteq \{A_{i_1} \sqcap \dots \sqcap A_{i_n} \sqsubseteq B_{i_1} \sqcap \dots \sqcap B_{i_m} \mid \{A_{i_1}, \dots, A_{i_n}, B_{i_1}, \dots, B_{i_m}\} \subseteq \Sigma\}$$

such that  $\mathcal{T} \cup \mathcal{H} \models C_1 \sqsubseteq C_2$  and  $\mathcal{T} \cap \mathcal{H} = \emptyset$ . The solution  $\mathcal{H}$  to the abduction problem is denoted as a hypothesis.

Note that since  $\mathcal{EL}$  TBoxes are always consistent, the consistency condition usually required on  $\mathcal{T} \cup \mathcal{H}$  is not needed here.

### 3 Limitation of Existing Criteria

We illustrate the problem that arises with the existing criteria in the following example. Given a TBox

$$\begin{aligned} \mathcal{T} = \{ & \exists \text{employment.ResearchPosition} \sqcap \exists \text{qualification.Diploma} \sqsubseteq \text{Researcher}, \\ & \exists \text{writes.ResearchPaper} \sqsubseteq \text{Researcher}, \text{Doctor} \sqsubseteq \exists \text{qualification.PhD}, \\ & \text{Professor} \equiv \text{Doctor} \sqcap \exists \text{employment.Chair}, \\ & \text{FundsProvider} \sqsubseteq \exists \text{writes.GrantApplication} \} \end{aligned}$$

and an observation  $\text{OBS} = \text{Professor} \sqsubseteq \text{Researcher}$ , the TBoxes

$$\begin{aligned} \mathcal{H}_1 &= \{ \text{Chair} \sqsubseteq \text{ResearchPosition}, \text{PhD} \sqsubseteq \text{Diploma} \} \text{ and} \\ \mathcal{H}_2 &= \{ \text{Professor} \sqsubseteq \text{FundsProvider}, \text{GrantApplication} \sqsubseteq \text{ResearchPaper} \} \end{aligned}$$

are solutions of the TBox abduction problem  $\langle \mathcal{T}, \mathbf{N}_{\mathcal{C}}, \text{OBS} \rangle$ . Note that both solutions are subset minimal, have the same size, and incomparable wrt. the entailment relation, so that traditional minimality criteria cannot distinguish them. However, intuitively, the second hypothesis feels more arbitrary than the first. Specifically, looking at  $\mathcal{H}_1$ ,  $\text{Chair}$  and  $\text{ResearchPosition}$  occur in  $\mathcal{T}$  in concept inclusions where the concepts in  $\text{OBS}$  also occur, and both  $\text{PhD}$  and  $\text{Diploma}$  are similarly related to  $\text{OBS}$  but via the role  $\text{qualification}$ . In contrast,  $\mathcal{H}_2$  involves the concepts  $\text{FundsProvider}$  and  $\text{GrantApplication}$  that are not related to  $\text{OBS}$  in any way in  $\mathcal{T}$ .

In fact, any random concept inclusion  $A \sqsubseteq \exists \text{writes}.B$  in  $\mathcal{T}$  would lead to a hypothesis similar to  $\mathcal{H}_2$  where  $A$  replaces  $\text{FundsProvider}$  and  $B$  replaces  $\text{GrantApplication}$ . Hence, the explanatory power of such hypotheses is very low. We need a minimality criterion that can discard hypotheses like  $\mathcal{H}_2$  if we want to keep only solutions with high explanatory potential.

### 4 Connection Minimal Abduction

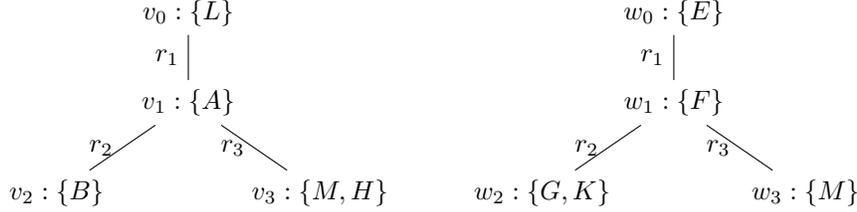
We introduce *connection minimality*, a minimality notion that rejects hypotheses connecting concepts in the observation without care for the existing entailment structure of the TBox. To represent this structure, we rely on the notion of an  $\mathcal{EL}$ -description tree, originally from Baader et al. [4], which basically correspond to syntax trees of  $\mathcal{EL}$  concepts, but ignoring the order of conjunction.

**Definition 2.** An  $\mathcal{EL}$ -description tree is a tree of the form  $T = (V, E, v_0, l)$  with root  $v_0 \in V$  where

- the nodes  $v \in V$  are labeled with  $l(v) \subseteq \mathbf{N}_C$ , and
- the (directed) edges  $vrw \in E$  are such that  $v, w \in V$  and are labeled with  $r \in \mathbf{N}_R$ .

Given such an  $\mathcal{EL}$ -description tree  $T$ , the corresponding concept  $C_T$  is defined recursively using  $C_T = C_{T, v_0}$  and  $C_{T, v} = \prod l(v) \sqcap \prod \{\exists r. C_{T, w} \mid vrw \in E\}$ .

*Example 3.* Let  $D_1 = L \sqcap \exists r_1. (A \sqcap \exists r_2. B \sqcap \exists r_3. (M \sqcap H))$  and  $D_2 = E \sqcap \exists r_1. (F \sqcap \exists r_2. (G \sqcap K) \sqcap \exists r_3. M)$ . The respective  $\mathcal{EL}$ -description trees representing these concepts are



To characterize connection minimal abduction, we map these trees to one another using the following “semantic” notion of homomorphisms.

**Definition 4.** Let  $T_1 = (V_1, E_1, v_0, l_1)$  and  $T_2 = (V_2, E_2, w_0, l_2)$  be  $\mathcal{EL}$ -description trees. A mapping  $\phi : V_2 \rightarrow V_1$  is a concept homomorphism from  $T_2$  to  $T_1$  w.r.t.  $\mathcal{T}$  if and only if the following conditions are satisfied:

1.  $\phi(w_0) = v_0$
2.  $\phi(v)r\phi(w) \in E_1$  for all  $vrw \in E_2$
3. for every  $v \in V_1$  and  $w \in V_2$  with  $v = \phi(w)$ ,  $\mathcal{T} \models \prod l_1(v) \sqsubseteq \prod l_2(w)$

Concept homomorphism w.r.t. a given TBox  $\mathcal{T}$  captures entailment w.r.t.  $\mathcal{T}$ : If  $\phi$  is a concept homomorphism from  $T_2$  to  $T_1$  w.r.t.  $\mathcal{T}$  then  $\mathcal{T} \models C_{T_1} \sqsubseteq C_{T_2}$ . This holds trivially from Point 1 and 3 of Definition 4.

*Example 5.* Consider again the trees  $T_1$  and  $T_2$  and respective concepts  $D_1 (= L \sqcap \exists r_1. (A \sqcap \exists r_2. B \sqcap \exists r_3. (M \sqcap H)))$  and  $D_2 (= E \sqcap \exists r_1. (F \sqcap \exists r_2. (G \sqcap K) \sqcap \exists r_3. M))$  from Example 3. Given the abduction problem  $\langle \mathcal{T}, \mathbf{N}_C, C_1 \sqsubseteq C_2 \rangle$ , where

$$\mathcal{T} = \{ C_1 \sqsubseteq D_1, D_2 \sqsubseteq C_2, A \sqsubseteq F, B \sqsubseteq G \},$$

and the TBox  $\mathcal{H} = \{ L \sqsubseteq E, B \sqsubseteq G \sqcap K \}$ , the function  $\phi$  such that  $\phi(w_i) = v_i$  is a concept homomorphism from  $T_2$  to  $T_1$  w.r.t.  $\mathcal{T} \cup \mathcal{H}$ . Thus  $\mathcal{T} \cup \mathcal{H} \models D_1 \sqsubseteq D_2$ . In addition  $\mathcal{T} \models C_1 \sqsubseteq D_1$  and  $\mathcal{T} \models D_2 \sqsubseteq C_2$ . Thus, the TBox  $\mathcal{H}$  is a hypothesis.

We use concept homomorphism to characterize entailment w.r.t. a given TBox—as in the example above—and to characterize hypotheses. To obtain our minimality notion, we additionally require solutions to avoid unnecessary conjuncts, which we do using the following two definitions.

**Definition 6.** Let  $C$  and  $D$  be concepts. Then  $C \preceq_{\sqcap} D$  if and only if:

- $D = C$ , or
- there exists  $D'$  and  $D''$  such that  $D = D' \sqcap D''$ , and  $C \preceq_{\sqcap} D'$ , or
- there exists  $r$ ,  $C'$  and  $D'$  such that  $C = \exists r.C'$ ,  $D = \exists r.D'$  and  $C' \preceq_{\sqcap} D'$ .

Intuitively,  $C \preceq_{\sqcap} D$  if we can remove any number of conjunct subexpressions from  $D$  to get  $C$ , e.g.,  $\exists r'.B \preceq_{\sqcap} \exists r.A \sqcap \exists r'.(B \sqcap B')$ .

**Definition 7.** Let  $C_1$  and  $C_2$  be concepts. A concept  $D$  connects  $C_1$  to  $C_2$  in  $\mathcal{T}$  if and only if  $\mathcal{T} \models C_1 \sqsubseteq D$  and  $\mathcal{T} \models D \sqsubseteq C_2$ . The connecting concept  $D$  is  $\preceq_{\sqcap}$ -minimal if all concepts  $D'$  that connect  $C_1$  to  $C_2$  in  $\mathcal{T}$  and verifying  $D' \preceq_{\sqcap} D$  are such that  $D \preceq_{\sqcap} D'$ .

For example, assume that both  $D = A \sqcap \exists r.B$  and  $D' = A \sqcap \exists r.(B \sqcap B')$  connect  $C_1$  and  $C_2$ . In that case, we prefer  $D$  because  $D \preceq_{\sqcap} D'$  but  $D' \not\preceq_{\sqcap} D$ . Note also that if either  $C_1$  or  $C_2$  does not connect  $C_1$  to  $C_2$  in  $\mathcal{T}$ , then no concept connects  $C_1$  to  $C_2$  in  $\mathcal{T}$ .

In Example 5, both  $D_1$  and  $D_2$  are connecting concepts in  $\mathcal{T} \cup \mathcal{H}$ , but  $D_1 (= L \sqcap \exists r_1.(A \sqcap \exists r_2.B \sqcap \exists r_3.(M \sqcap H)))$  is not  $\preceq_{\sqcap}$ -minimal, because  $D'_1 = L \sqcap \exists r_1.(A \sqcap \exists r_2.B \sqcap \exists r_3.M)$  is such that  $D'_1 \preceq_{\sqcap} D_1$  and it also connects  $C_1$  to  $C_2$  in  $\mathcal{T} \cup \mathcal{H}$ . In fact,  $D'_1$  as well as  $D_2$  are  $\preceq_{\sqcap}$ -minimal.

Intuitively, our characterization of minimal hypotheses for abduction problems  $\langle \mathcal{T}, \Sigma, C_1 \sqsubseteq C_2 \rangle$  works as follows. As any hypothesis,  $\mathcal{H}$  turns some subsumer  $C_{T_1}$  of  $C_1$  and some subsumee  $C_{T_2}$  of  $C_2$  into connecting concepts from  $C_1$  to  $C_2$  (for some  $\mathcal{EL}$ -description trees  $T_1$  and  $T_2$ ). We require that  $C_{T_1}$  and  $C_{T_2}$  are  $\preceq_{\sqcap}$ -minimal, and thus contain no unnecessary conjuncts. Furthermore, we require that the connection between  $C_{T_1}$  and  $C_{T_2}$  is characterized by a concept homomorphism, and that  $\mathcal{H}$  contains only GCIs that are required for this connection to hold. This last condition reflects our idea of *minimal connectedness* motivated in Section 3.

**Definition 8 (Connection Minimal Abduction).** Given an abduction problem  $\langle \mathcal{T}, \Sigma, C_1 \sqsubseteq C_2 \rangle$ , the hypothesis  $\mathcal{H}$  is connection minimal if and only if there exist  $\mathcal{EL}$ -description trees  $T_1 = (V_1, E_1, v_1, l_1)$  and  $T_2 = (V_2, E_2, v_2, l_2)$  s.t.

1.  $\mathcal{T} \models C_1 \sqsubseteq C_{T_1}, C_{T_2} \sqsubseteq C_2$ ,
2.  $C_{T_1}$  and  $C_{T_2}$  are  $\preceq_{\sqcap}$ -minimal connecting concepts from  $C_1$  to  $C_2$  in  $\mathcal{T} \cup \mathcal{H}$ ,
3. there is a concept homomorphism  $\phi$  from  $T_1$  to  $T_2$  w.r.t.  $\mathcal{T} \cup \mathcal{H}$ , s.t.  $\mathcal{H} = \{ \prod l_1(v) \sqsubseteq \prod l_2(w) \mid w \in V_2, v = \phi(w), \mathcal{T} \not\models \prod l_1(v) \sqsubseteq \prod l_2(w) \}$ .

Returning to Example 5,  $D'_1$  and  $D_2$  satisfy all the requirements of connection minimality, thus the hypothesis  $\mathcal{H} = \{L \sqsubseteq E, B \sqsubseteq G \sqcap K\}$  is minimal. This definition also rejects  $\mathcal{H}_2$  from Section 3 because it is impossible to find  $T_1$  and  $T_2$  verifying points 1 and 2 of Definition 8. However  $\mathcal{H}_1$  is accepted. The connecting concepts  $D_1 = \exists \text{employment.Chair} \sqcap \exists \text{qualification.PhD}$  and  $D_2 = \exists \text{employment.ResearchPosition} \sqcap \exists \text{qualification.Diploma}$  are the witnesses attesting that  $\mathcal{H}_1$  is a connection minimal hypothesis.

This new notion of minimality achieves our aim of discriminating the more arbitrary solutions. It remains to compute it efficiently. We believe this can be achieved via a translation to first-order logic, but a proper investigation remains to be conducted.

## References

1. Alrabbaa, C., Baader, F., Borgwardt, S., Koopmann, P., Kovtunova, A.: Finding small proofs for description logic entailments: Theory and practice. In: Albert, E., Kovacs, L. (eds.) LPAR-23: 23rd International Conference on Logic for Programming, Artificial Intelligence and Reasoning. EPiC Series in Computing, vol. 73, pp. 32–67. EasyChair (2020). <https://doi.org/10.29007/nhpp>
2. Alrabbaa, C., Baader, F., Borgwardt, S., Koopmann, P., Kovtunova, A.: Finding good proofs for description logic entailments using recursive quality measures. In: Proceedings of the 28th International Conference on Automated Deduction (CADE-28), July 11–16, 2021, Virtual Event, United States (2021), to appear.
3. Baader, F., Horrocks, I., Lutz, C., Sattler, U.: An Introduction to Description Logic. Cambridge University Press (2017). <https://doi.org/10.1017/9781139025355>
4. Baader, F., Küsters, R., Molitor, R.: Computing least common subsumers in description logics with existential restrictions. In: Proceedings of IJCAI 1999. pp. 96–103. Morgan Kaufmann (1999)
5. Baader, F., Suntisrivaraporn, B.: Debugging SNOMED CT using axiom pinpointing in the description logic  $\mathcal{EL}^+$ . In: Proc. of the 3rd Conference on Knowledge Representation in Medicine (KR-MED’08): Representing and Sharing Knowledge Using SNOMED. CEUR-WS, vol. 410 (2008), <http://ceur-ws.org/Vol-410/Paper01.pdf>
6. Bauer, J., Sattler, U., Parsia, B.: Explaining by example: Model exploration for ontology comprehension. In: Grau, B.C., Horrocks, I., Motik, B., Sattler, U. (eds.) Proceedings of the 22nd International Workshop on Description Logics (DL 2009), Oxford, UK, July 27–30, 2009. CEUR Workshop Proceedings, vol. 477. CEUR-WS.org (2009), [http://ceur-ws.org/Vol-477/paper\\_37.pdf](http://ceur-ws.org/Vol-477/paper_37.pdf)
7. Bienvenu, M.: Complexity of abduction in the  $\mathcal{EL}$  family of lightweight description logics. In: Proceedings of KR 2008. pp. 220–230. AAAI Press (2008), <http://www.aaai.org/Library/KR/2008/kr08-022.php>
8. Calvanese, D., Ortiz, M., Simkus, M., Stefanoni, G.: Reasoning about explanations for negative query answers in DL-Lite. J. Artif. Intell. Res. **48**, 635–669 (2013). <https://doi.org/10.1613/jair.3870>
9. Ceylan, İ.İ., Lukasiewicz, T., Malizia, E., Molinaro, C., Vaicenavicius, A.: Explanations for negative query answers under existential rules. In: Calvanese, D., Erdem, E., Thielscher, M. (eds.) Proceedings of KR 2020. pp. 223–232. AAAI Press (2020). <https://doi.org/10.24963/kr.2020/23>
10. Del-Pinto, W., Schmidt, R.A.: ABox abduction via forgetting in  $\mathcal{ALC}$ . In: The Thirty-Third AAAI Conference on Artificial Intelligence, AAAI 2019. pp. 2768–2775. AAAI Press (2019). <https://doi.org/10.1609/aaai.v33i01.33012768>
11. Du, J., Qi, G., Shen, Y., Pan, J.Z.: Towards practical ABox abduction in large description logic ontologies. Int. J. Semantic Web Inf. Syst. **8**(2), 1–33 (2012). <https://doi.org/10.4018/jswis.2012040101>
12. Du, J., Wan, H., Ma, H.: Practical TBox abduction based on justification patterns. In: Proceedings of the Thirty-First AAAI Conference on Artificial Intelligence. pp. 1100–1106 (2017), <http://aaai.org/ocs/index.php/AAAI/AAAI17/paper/view/14402>
13. Du, J., Wan, H., Ma, H.: Practical TBox abduction based on justification patterns. In: Proceedings of the Thirty-First AAAI Conference on Artificial Intelligence. pp. 1100–1106 (2017), <http://aaai.org/ocs/index.php/AAAI/AAAI17/paper/view/14402>

14. Du, J., Wang, K., Shen, Y.: A tractable approach to ABox abduction over description logic ontologies. In: Brodley, C.E., Stone, P. (eds.) Proceedings of the Twenty-Eighth AAAI Conference on Artificial Intelligence. pp. 1034–1040. AAAI Press (2014), <http://www.aaai.org/ocs/index.php/AAAI/AAAI14/paper/view/8191>
15. Elsenbroich, C., Kutz, O., Sattler, U.: A case for abductive reasoning over ontologies. In: Proceedings of the OWLED’06 Workshop on OWL: Experiences and Directions (2006), [http://ceur-ws.org/Vol-216/submission\\_25.pdf](http://ceur-ws.org/Vol-216/submission_25.pdf)
16. Halland, K., Britz, K.: ABox abduction in  $\mathcal{ALC}$  using a DL tableau. In: 2012 South African Institute of Computer Scientists and Information Technologists Conference, SAICSIT ’12. pp. 51–58 (2012). <https://doi.org/10.1145/2389836.2389843>
17. Horridge, M.: Justification Based Explanation in Ontologies. Ph.D. thesis, University of Manchester, UK (2011), [https://www.research.manchester.ac.uk/portal/files/54511395/FULL\\_TEXT.PDF](https://www.research.manchester.ac.uk/portal/files/54511395/FULL_TEXT.PDF)
18. Horridge, M., Parsia, B., Sattler, U.: Explanation of OWL entailments in protege 4. In: Bizer, C., Joshi, A. (eds.) Proceedings of the Poster and Demonstration Session at the 7th International Semantic Web Conference (ISWC2008), Karlsruhe, Germany, October 28, 2008. CEUR Workshop Proceedings, vol. 401. CEUR-WS.org (2008), [http://ceur-ws.org/Vol-401/iswc2008pd\\_submission\\_47.pdf](http://ceur-ws.org/Vol-401/iswc2008pd_submission_47.pdf)
19. Kazakov, Y., Klinov, P., Stupnikov, A.: Towards reusable explanation services in protege. In: Artale, A., Glimm, B., Kontchakov, R. (eds.) Proceedings of the 30th International Workshop on Description Logics, Montpellier, France, July 18–21, 2017. CEUR Workshop Proceedings, vol. 1879. CEUR-WS.org (2017), <http://ceur-ws.org/Vol-1879/paper31.pdf>
20. Klarman, S., Endriss, U., Schlobach, S.: ABox abduction in the description logic  $\mathcal{ALC}$ . Journal of Automated Reasoning **46**(1), 43–80 (2011). <https://doi.org/10.1007/s10817-010-9168-z>
21. Koopmann, P.: Signature-based abduction with fresh individuals and complex concepts for description logics. In: Zhou, Z. (ed.) Proceedings of the Thirtieth International Joint Conference on Artificial Intelligence, IJCAI 2021, Virtual Event / Montreal, Canada, 19–27 August 2021. pp. 1929–1935. ijcai.org (2021). <https://doi.org/10.24963/ijcai.2021/266>
22. Koopmann, P., Del-Pinto, W., Tournet, S., Schmidt, R.A.: Signature-based abduction for expressive description logics. In: Calvanese, D., Erdem, E., Thielscher, M. (eds.) Proceedings of the 17th International Conference on Principles of Knowledge Representation and Reasoning, KR 2020. pp. 592–602. AAAI Press (2020). <https://doi.org/10.24963/kr.2020/59>
23. Parsia, B., Matentzoglou, N., Gonçalves, R.S., Glimm, B., Steigmiller, A.: The OWL reasoner evaluation (ORE) 2015 competition report. J. Autom. Reason. **59**(4), 455–482 (2017). <https://doi.org/10.1007/s10817-017-9406-8>
24. Pukancová, J., Homola, M.: Tableau-based ABox abduction for the  $\mathcal{ALCHO}$  description logic. In: Proceedings of the 30th International Workshop on Description Logics (2017), <http://ceur-ws.org/Vol-1879/paper11.pdf>
25. Pukancová, J., Homola, M.: The AAA ABox abduction solver. Künstliche Intell. **34**(4), 517–522 (2020). <https://doi.org/10.1007/s13218-020-00685-4>
26. Schlobach, S., Cornet, R.: Non-standard reasoning services for the debugging of description logic terminologies. In: Gottlob, G., Walsh, T. (eds.) Proc. of the 18th Int. Joint Conf. on Artificial Intelligence (IJCAI 2003). pp. 355–362. Morgan Kaufmann, Acapulco, Mexico (2003), <http://ijcai.org/Proceedings/03/Papers/053.pdf>
27. Wei-Kleiner, F., Dragisic, Z., Lambrix, P.: Abduction framework for repairing incomplete  $\mathcal{EL}$  ontologies: Complexity results and algorithms. In: Proceedings of

the Twenty-Eighth AAAI Conference on Artificial Intelligence. pp. 1120–1127. AAAI Press (2014), <http://www.aaai.org/ocs/index.php/AAAI/AAAI14/paper/view/8239>