

5. Exercises for the Course 'Description Logics'

Exercise 18:

Extend the proof of Lemma 4.1 (local correctness) to the \sqcap -rule and the \forall -rule.

Exercise 19:

Use the tableau algorithm from the lecture to decide whether the following subsumption holds:

$$\neg\forall r.A \sqcap \forall r.C \sqsubseteq_{\mathcal{T}} \forall r.E$$

where $\mathcal{T} = \{C \equiv (\exists r.\neg B) \sqcap \neg A, \quad D \equiv \exists r.B, \quad E \equiv \neg(\exists r.A) \sqcap \exists r.D\}$.

Exercise 20:

Prove by induction Lemma 4.5 from the lecture.

Exercise 21:

Prove Lemma 4.6 from the lecture.