

Faculty of Computer Science Institute of Theoretical Computer Science, Chair of Automata Theory

# **Description Logics**

## **Exercise Sheet 5**

Dr. Anni-Yasmin Turhan / Dipl.-Math. Felix Distel Summer Semester 2011

### Exercise 1

Extend the proof of Lemma 4.1 (local correctness) to the ⊓-rule and the ∀-rule.

# Exercise 2

Use the tableau algorithm from the lecture to decide whether the following subsumption holds:

 $\neg \forall r. A \sqcap \forall r. C \sqsubseteq_{\mathcal{T}} \forall r. E$ 

where  $\mathcal{T} = \{ C \equiv (\exists r. \neg B) \sqcap \neg A, D \equiv \exists r. B, E \equiv \neg (\exists r. A) \sqcap \exists r. D \}.$ 

### Exercise 3

Prove by induction Lemma 4.5 from the lecture.

#### Exercise 4

Prove Lemma 4.6 from the lecture.