

15. Exercises for the Course „Logic-based Knowledge Representation“

Exercise 50:

$$(a) \text{ Let } D := \left\{ \frac{\text{Italian}(x) : \text{lovesWine}(x)}{\text{lovesWine}(x)}, \frac{\text{French}(x) : \text{lovesWine}(x)}{\text{lovesWine}(x)} \right\}$$
$$W := \{ \text{Italian}(\text{Tom}) \vee \text{French}(\text{Tom}) \} .$$

Compute the extensions of D and W and decide whether Tom loves wine.

$$(b) \text{ Let } D := \left\{ \frac{\text{true} : \text{usable}(x) \wedge \neg \text{broken}(x)}{\text{usable}(x)} \right\}$$
$$W := \{ \text{broken}(\text{leftArm}) \vee \text{broken}(\text{rightArm}) \} .$$

Compute the extensions of D and W and decide whether both arms are usable.

Exercise 51:

Consider the default theory (D, W) from Example 8.5 of the lecture: for closed atomic formulae a, b, c of first order predicate logic, we define

$$D := \left\{ \frac{a : b}{c}, \frac{c : \neg b}{\neg b} \right\}$$
$$W := \{ a \} .$$

Prove that (D, W) has no extension.

Exercise 52:

Let (D, W) be a default theory.

- Let $\mathcal{E}_{(D,W)}$ be the set of all extensions of (D, W) .
- We call $E, E' \in \mathcal{E}_{(D,W)}$ *incomparable*, if neither $E \subseteq E'$ nor $E' \subseteq E$.

Prove or disprove the following claims:

- (a) There exists a default theory (D, W) with $|\mathcal{E}_{(D,W)}| \geq 2$ and where all $E, E' \in \mathcal{E}_{(D,W)}$ with $E \neq E'$ are incomparable.
- (b) There exists a default theory (D, W) with $|\mathcal{E}_{(D,W)}| \geq 2$ and where, for all $E, E' \in \mathcal{E}_{(D,W)}$, either $E \subseteq E'$ or $E' \subseteq E$.

Exercise 53:

Let Π be a ground logic program without NAF. Prove that, if Γ is the (non-empty) set of all models of Π , then $\bigcap \Gamma$ is also a model of Π .