

# Reasoning in Description Logic Ontologies for Privacy Management

Adrian Nuradiansyah

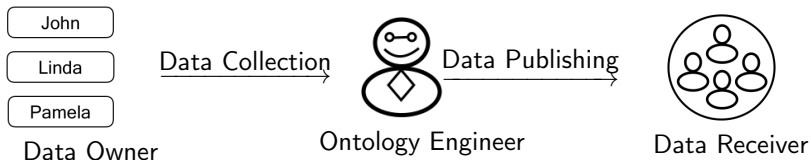
**Technische Universität Dresden**

October 6, 2020



# Data Collection and Data Publishing for Ontologies

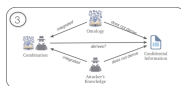
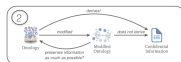
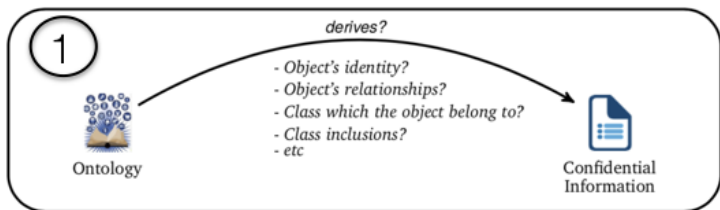
What [Fung et. al, 2010] illustrate ...



In the context of Description Logic Ontologies, [Grau, 2010] concerns ...

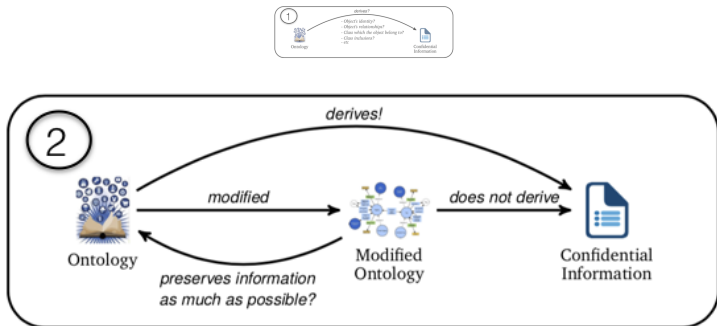
- A rise in the number of ontologies integrated in mainstream applications, e.g., medical systems
- Possible **unauthorized disclosures** of medical information may occur
- Designing privacy-preserving systems is being a critical requirement

# What Should the Engineer Do Before Publishing?



Detect Privacy Breach

# What Should the Engineer Do Before Publishing?

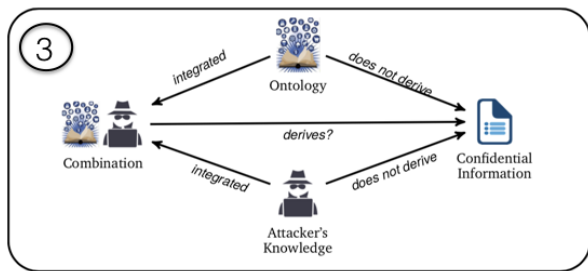
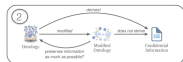
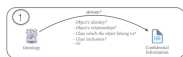


Detect Privacy Breach



Ontology Repair

# What Should the Engineer Do Before Publishing?



Detect Privacy Breach



Ontology Repair



Avoid ILnkgage Attacks

# What People Have Done



- Confidential information  $\Rightarrow$  *property of individuals*
- Membership of individuals (tuple of individuals) in the answers to certain queries  
(e.g., [Calvanesse et. al., 2008], [Stouppa & Studer, 2009], [Tao et.al., 2010] )

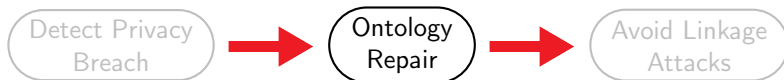
# What People Have Done



- Confidential information  $\Rightarrow$  *property of individuals*
- Membership of individuals (tuple of individuals) in the answers to certain queries  
(e.g., [Calvanese et. al., 2008], [Stouppa & Studer, 2009], [Tao et.al., 2010] )

*Focus on Identity? What is "identity"?*

# What People Have Done



- Finding justifications why the (unwanted) consequences can be derived (e.g., [Schlobach, 2003], [Parsia et. al., 2007], [Baader et. al., 2008])
- Remove axioms that are responsible for the entailment (e.g., [Kalyanpur et. al., 2006])



# What People Have Done



- Finding justifications why the (unwanted) consequences can be derived (e.g., [Schlobach, 2003], [Parsia et. al., 2007], [Baader et. al., 2008])
- Remove axioms that are responsible for the entailment (e.g., [Kalyanpur et. al., 2006])

*Do these approaches also remove useful consequences?  
Can we do it more "gentle"?*

# What People Have Done



- Learning type of attackers' background knowledge
- Investigating *attribute linkage*, *table linkage*, etc thoroughly in e.g., [Fung et. al., 2010]
- Introducing the notion of *policy-compliance and policy-safety* in the context of RDF graphs/Linked Data in e.g., [Grau & Kostylev, 2016]

# What People Have Done



- Learning type of attackers' background knowledge
- Investigating *attribute linkage*, *table linkage*, etc thoroughly in e.g., [Fung et. al., 2010]
- Introducing the notion of *policy-compliance and policy-safety* in the context of RDF graphs/Linked Data in e.g., [Grau & Kostylev, 2016]

*Is such setting already considered in DL ontologies?*

Detecting Privacy Breach

The Identity Problem and its Variants  
in Description Logic Ontologies

Ontology Repair

Repairing Description Logic Ontologies  
via Axiom Weakening

Avoiding Linkage Attacks

Privacy-Preserving Ontology Publishing

# Description Logics (DLs)

The **logical underpinning** of **Web Ontology Language (OWL)**

Decidable fragments of First Order Logics

Representing the conceptual knowledge of an application domain in a well-understood way.

# Description Logics (DLs)

The **logical underpinning** of **Web Ontology Language (OWL)**

Decidable fragments of First Order Logics

Representing the conceptual knowledge of an application domain in a well-understood way.

*Non-German people who work at an IT Department whose all locations are either in Germany or in Austria*



$\neg \text{German} \sqcap \exists \text{worksAt} . (\text{ITDept} \sqcap \forall \text{located} . (\text{Germany} \sqcup \text{Austria}))$

Name	Syntax	Example
Top	$\top$	<i>tautology</i>
Concept Name	$A$	<i>Germany</i>
Conjunction	$C \sqcap D$	<i>German</i> $\sqcap$ <i>Female</i>
Disjunction	$C \sqcup D$	<i>Germany</i> $\sqcup$ <i>Austria</i>
Existential Restriction	$\exists r.C$	<i>German</i> $\sqcap$ $\exists$ <i>worksAt.ITDept</i>
Universal Restriction	$\forall r.C$	<i>ITDept</i> $\sqcap$ $\forall$ <i>located.Germany</i>
Negation	$\neg C$	$\neg$ <i>German</i>
(One of) Nominal	$\{a_1, \dots, a_n\}$	$\{LINDA, JOHN, JIM\}$

Name	Syntax	Example
Top	$\top$	<i>tautology</i>
Concept Name	$A$	<i>Germany</i>
Conjunction	$C \sqcap D$	<i>German</i> $\sqcap$ <i>Female</i>
Disjunction	$C \sqcup D$	<i>Germany</i> $\sqcup$ <i>Austria</i>
Existential Restriction	$\exists r.C$	<i>German</i> $\sqcap$ $\exists$ <i>worksAt.ITDept</i>
Universal Restriction	$\forall r.C$	<i>ITDept</i> $\sqcap$ $\forall$ <i>located.Germany</i>
Negation	$\neg C$	$\neg$ <i>German</i>
(One of) Nominal	$\{a_1, \dots, a_n\}$	$\{LINDA, JOHN, JIM\}$

*ALC*

- Closed under Boolean operators
- Intractable



Name	Syntax	Example
Top	$\top$	<i>tautology</i>
Concept Name	$A$	<i>Germany</i>
Conjunction	$C \sqcap D$	<i>German</i> $\sqcap$ <i>Female</i>
Disjunction	$C \sqcup D$	<i>Germany</i> $\sqcup$ <i>Austria</i>
Existential Restriction	$\exists r.C$	<i>German</i> $\sqcap$ $\exists$ <i>worksAt.ITDept</i>
Universal Restriction	$\forall r.C$	<i>ITDept</i> $\sqcap$ $\forall$ <i>located.Germany</i>
Negation	$\neg C$	$\neg$ <i>German</i>
(One of) Nominal	$\{a_1, \dots, a_n\}$	$\{LINDA, JOHN, JIM\}$

 $\mathcal{EL}$ 

inexpressive, but reasoning is in PTime

Name	Syntax	Example
Top	$\top$	<i>tautology</i>
Concept Name	$A$	<i>Germany</i>
Conjunction	$C \sqcap D$	<i>German</i> $\sqcap$ <i>Female</i>
Disjunction	$C \sqcup D$	<i>Germany</i> $\sqcup$ <i>Austria</i>
Existential Restriction	$\exists r.C$	<i>German</i> $\sqcap$ $\exists$ <i>worksAt.ITDept</i>
Universal Restriction	$\forall r.C$	<i>ITDept</i> $\sqcap$ $\forall$ <i>located.Germany</i>
Negation	$\neg C$	$\neg$ <i>German</i>
(One of) Nominal	$\{a_1, \dots, a_n\}$	$\{LINDA, JOHN, JIM\}$

 $\mathcal{FL}_0$ The dual of  $\mathcal{EL}$

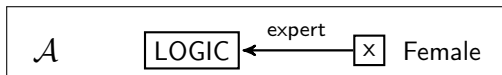
Name	Syntax	Example
Top	$\top$	<i>tautology</i>
Concept Name	$A$	<i>Germany</i>
Conjunction	$C \sqcap D$	<i>German</i> $\sqcap$ <i>Patient</i>
Disjunction	$C \sqcup D$	<i>Germany</i> $\sqcup$ <i>Austria</i>
Existential Restriction	$\exists r.C$	<i>German</i> $\sqcap$ $\exists$ <i>worksAt.ITDept</i>
Universal Restriction	$\forall r.C$	<i>ITDept</i> $\sqcap$ $\forall$ <i>located.Germany</i>
Negation	$\neg C$	$\neg$ <i>German</i>
(One of) Nominal	$\{a_1, \dots, a_n\}$	$\{LINDA, JOHN, JIM\}$

 $\mathcal{FL}\mathcal{E}$ Combination of  $\mathcal{EL}$  and  $\mathcal{FL}_0$

A **DL ontology**  $\mathfrak{D}$  consists of an **ABox**  $\mathcal{A}$  and a **TBox**  $\mathcal{T} \iff \mathfrak{D} = (\mathcal{A}, \mathcal{T})$

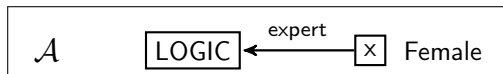
A **DL ontology**  $\mathcal{D}$  consists of an **ABox**  $\mathcal{A}$  and a **TBox**  $\mathcal{T} \iff \mathcal{D} = (\mathcal{A}, \mathcal{T})$

An ABox  $\mathcal{A}$ : **knowledge about individuals** (instance relationships  $C(a)$  and individual relationships  $r(a, b)$ )

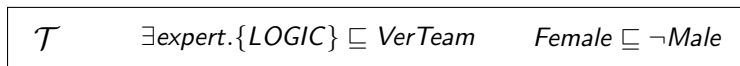


A **DL ontology**  $\mathcal{D}$  consists of an **ABox**  $\mathcal{A}$  and a **TBox**  $\mathcal{T} \iff \mathcal{D} = (\mathcal{A}, \mathcal{T})$

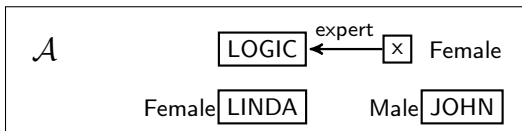
An ABox  $\mathcal{A}$ : **knowledge about individuals** (instance relationships  $C(a)$  and individual relationships  $r(a, b)$ )



A TBox  $\mathcal{T}$ : inclusion relationships/constraints between concepts  $C \sqsubseteq D$  (**General Concept Inclusions (GCIs)**)

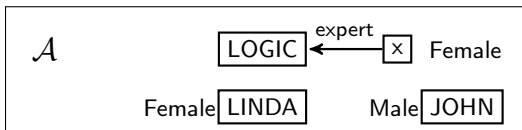


# What can I Infer from an Ontology?



$\mathcal{T}$   $\exists \text{expert}.\{\text{LOGIC}\} \sqsubseteq \text{VerTeam}$      $\text{Female} \sqsubseteq \neg \text{Male}$   
 $\text{VerTeam} \equiv \{\text{LINDA}, \text{JOHN}\}$

# What can I Infer from an Ontology?



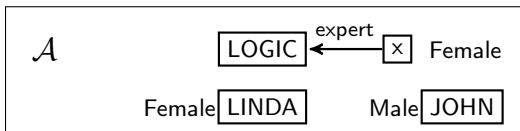
$\mathcal{T}$   $\exists \text{expert}.\{\text{LOGIC}\} \sqsubseteq \text{VerTeam}$      $\text{Female} \sqsubseteq \neg \text{Male}$   
 $\text{VerTeam} \equiv \{\text{LINDA}, \text{JOHN}\}$

Does  $\exists \text{expert}.\{\text{LOGIC}\} \sqsubseteq \{\text{LINDA}, \text{JOHN}\}$  hold  
w.r.t.  $(\mathcal{A}, \mathcal{T})$ ?  $\checkmark$  (**Subsumption Problem**)

Is  $x$  an instance of  $\text{VerTeam}$   
w.r.t.  $(\mathcal{A}, \mathcal{T})$ ?  $\checkmark$  (**Instance Problem**)



# What can I Infer from an Ontology?



$\mathcal{T} \quad \exists \text{expert}.\{\text{LOGIC}\} \sqsubseteq \text{VerTeam} \quad \text{Female} \sqsubseteq \neg \text{Male}$   
 $\text{VerTeam} \equiv \{\text{LINDA}, \text{JOHN}\}$

Does  $\exists \text{expert}.\{\text{LOGIC}\} \sqsubseteq \{\text{LINDA}, \text{JOHN}\}$  hold  
w.r.t.  $(\mathcal{A}, \mathcal{T})$ ?  $\checkmark$  (**Subsumption Problem**)

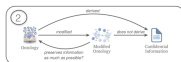
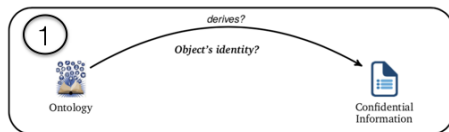
Is  $x$  an instance of  $\text{VerTeam}$   
w.r.t.  $(\mathcal{A}, \mathcal{T})$ ?  $\checkmark$  (**Instance Problem**)

Is LINDA the **identity**  
of anonymous  $x$ ?  $\checkmark$

Wait, how do  
you know it?

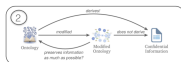
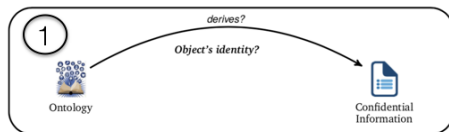
how do we call this  
problem?

# Problem 1: Is My Identity Safe?



Identity Problem ( $\mathcal{D} \models x \doteq a$ ) [DL 2017], [JIST 2017]

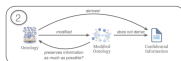
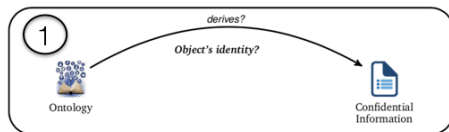
# Problem 1: Is My Identity Safe?



## Identity Problem ( $\mathcal{D} \models x \doteq a$ ) [DL 2017], [JIST 2017]

- Not all DLs are able to derive equalities between individuals, e.g.  $\mathcal{ALC}$ .
- **DLs with equality power:** nominals, number restrictions, and functional dependencies.

# Problem 1: Is My Identity Safe?

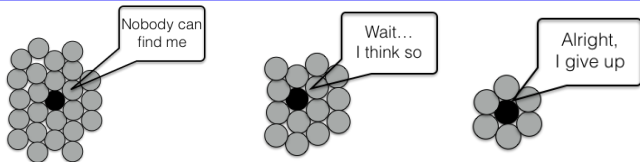


## Identity Problem ( $\mathcal{D} \models x \doteq a$ ) [DL 2017], [JIST 2017]

- Not all DLs are able to derive equalities between individuals, e.g.  $\mathcal{ALC}$ .
- **DLs with equality power:** nominals, number restrictions, and functional dependencies.
- **Identity to Instance:** Given two individuals  $x, a$ , and an ontology  $\mathcal{D}$  formulated in a DL with equality power, it holds

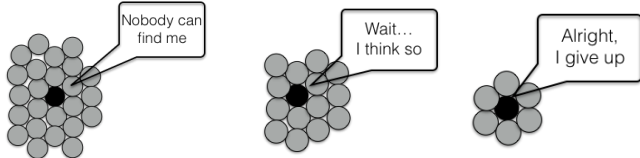
$\mathcal{D} \models x \doteq a$  iff  $(\mathcal{D} \cup \{Q(x)\}) \models Q(a)$ , where  $Q$  is a fresh concept name

# The Identity is one of $k$ Known Individuals



*"Hiding in the crowd" ...*

# The Identity is one of $k$ Known Individuals



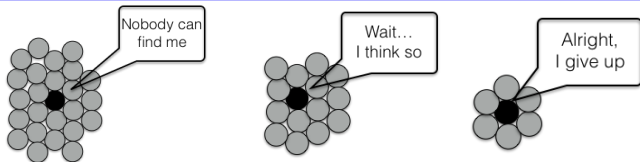
*"Hiding in the crowd" ...*

## $k$ -Hiding

The anonymous individual  $x$  is **not  $k$ -hidden** w.r.t.  $\mathcal{D}$  iff there are known individuals  $a_1, \dots, a_{k-1}$  such that

$x$  belongs to  $\{a_1, \dots, a_{k-1}\}$  w.r.t.  $\mathcal{D}$

# The Identity is one of $k$ Known Individuals



*"Hiding in the crowd" ...*

## $k$ -Hiding

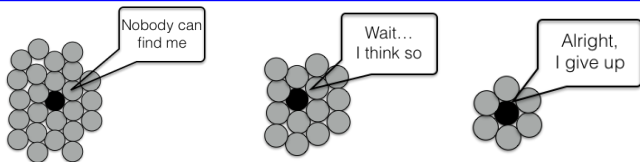
The anonymous individual  $x$  is **not  $k$ -hidden** w.r.t.  $\mathcal{D}$  iff there are known individuals  $a_1, \dots, a_{k-1}$  such that

$x$  belongs to  $\{a_1, \dots, a_{k-1}\}$  w.r.t.  $\mathcal{D}$

## How to solve it

- Reduce it to the instance problem for *all* DLs with equality power
- Reduce it to the identity problem for *some* convex DLs with equality power

# The Identity is one of $k$ Known Individuals



*"Hiding in the crowd" ...*

## $k$ -Hiding

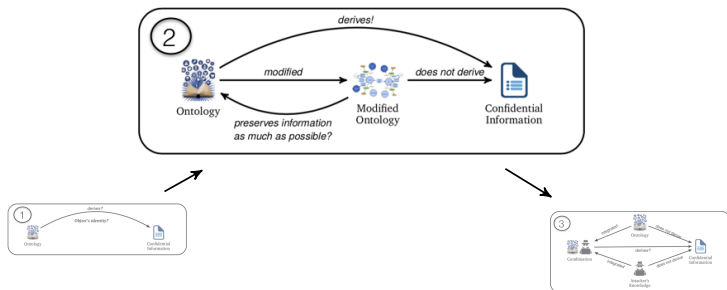
The anonymous individual  $x$  is **not  $k$ -hidden** w.r.t.  $\mathcal{D}$  iff there are known individuals  $a_1, \dots, a_{k-1}$  such that

$x$  belongs to  $\{a_1, \dots, a_{k-1}\}$  w.r.t.  $\mathcal{D}$

*If (variants) of the identity problem can be reduced to classical reasoning problems in DLs, then now let's consider **more general types of confidential axioms** (e.g., instance relationships, subsumptions, CQs, etc).*



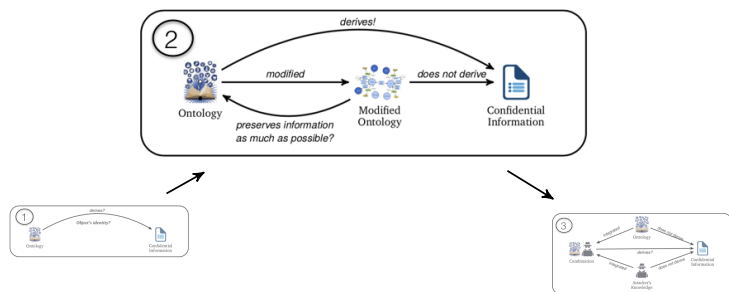
# Problem 2: How to Protect the Confidential Information?



## Ontology Repair ([KR 2018], [DL 2018])

- $\mathcal{D} = \mathcal{D}_s \cup \mathcal{D}_r$ , where  $\mathcal{D}_s$  is a **static ontology** and  $\mathcal{D}_r$  is a **refutable ontology**.
- Let  $Con(\mathcal{D}) := \{\alpha \mid \mathcal{D} \models \alpha\}$  be the set of all **consequences** of  $\mathcal{D}$ .

# Problem 2: How to Protect the Confidential Information?

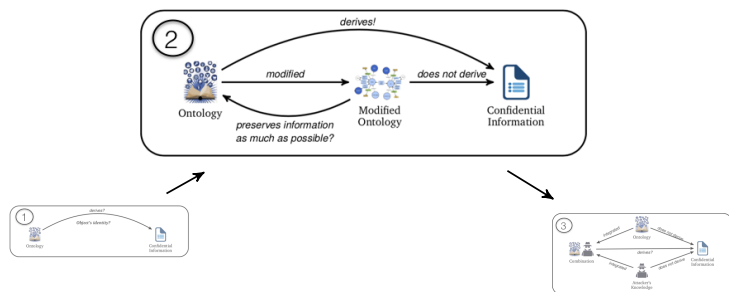


## Ontology Repair ([KR 2018], [DL 2018])

- $\mathcal{D} = \mathcal{D}_s \cup \mathcal{D}_r$ , where  $\mathcal{D}_s$  is a **static ontology** and  $\mathcal{D}_r$  is a **refutable ontology**.
- Let  $Con(\mathcal{D}) := \{\alpha \mid \mathcal{D} \models \alpha\}$  be the set of all **consequences** of  $\mathcal{D}$ .
- Let  $\mathcal{D} \models \alpha$  and  $\mathcal{D}_s \not\models \alpha$ . The ontology  $\mathcal{D}'$  is a **repair** of  $\mathcal{D}$  w.r.t.  $\alpha$

$$Con(\mathcal{D}_s \cup \mathcal{D}') \subseteq Con(\mathcal{D}) \setminus \{\alpha\}$$

# Problem 2: How to Protect the Confidential Information?



## Ontology Repair ([KR 2018], [DL 2018])

- $\mathcal{D} = \mathcal{D}_s \cup \mathcal{D}_r$ , where  $\mathcal{D}_s$  is a **static ontology** and  $\mathcal{D}_r$  is a **refutable ontology**.
- Let  $Con(\mathcal{D}) := \{\alpha \mid \mathcal{D} \models \alpha\}$  be the set of all **consequences** of  $\mathcal{D}$ .
- Let  $\mathcal{D} \models \alpha$  and  $\mathcal{D}_s \not\models \alpha$ . The ontology  $\mathcal{D}'$  is a **repair** of  $\mathcal{D}$  w.r.t.  $\alpha$

$$Con(\mathcal{D}_s \cup \mathcal{D}') \subseteq Con(\mathcal{D}) \setminus \{\alpha\}$$

- **Optimal repair**  $\mathcal{D}'$  of  $\mathcal{D}$  w.r.t.  $\alpha$ :  
No Repair  $\mathcal{D}''$  of  $\mathcal{D}$  w.r.t.  $\alpha$  such that  $Con(\mathcal{D}' \cup \mathcal{D}_s) \subset Con(\mathcal{D}'' \cup \mathcal{D}_s)$ .

# Optimal Classical Repairs

Optimal Repairs need not exist in general!

## Optimal Classical Repair

A maximum subset  $\mathcal{D}'$  of  $\mathcal{D}_r$  such that  $\mathcal{D}_s \cup \mathcal{D}' \neq \alpha$

# Optimal Classical Repairs

Optimal Repairs need not exist in general!

## Optimal Classical Repair

A maximum subset  $\mathcal{D}'$  of  $\mathcal{D}_r$  such that  $\mathcal{D}_s \cup \mathcal{D}' \not\models \alpha$

- Optimal classical repairs always exist  $\rightarrow$  **Justification** and **Hitting Set (Reiter, 1987)**
- Let  $\mathcal{D} \models \alpha$ . A **justification**  $J$  of  $\mathcal{D}$  w.r.t.  $\alpha$  is a minimal subset of  $\mathcal{D}_r$  s.t.  $\mathcal{D}_s \cup J \models \alpha$ .
- Let  $J_1, \dots, J_k$  be the justifications of  $\mathcal{D}$  w.r.t.  $\alpha$ .  
A **hitting set**  $\mathcal{H}$  of these justifications is a set of axioms such that  $\mathcal{H} \cap J_i \neq \emptyset$
- A hitting set  $\mathcal{H}_{min}$  is **minimal** if there is no  $\mathcal{H}'$  of  $J_1, \dots, J_k$  such that  $\mathcal{H}' \subset \mathcal{H}_{min}$ .
- $\mathcal{D}' := \mathcal{D}_r \setminus \mathcal{H}_{min}$  is an **optimal classical repair** of  $\mathcal{D}$  w.r.t.  $\alpha$  such that

$$\mathcal{D}_s \cup \mathcal{D}' \not\models \alpha$$

# Gentle Repair

Obtaining Classical Repairs  $\rightarrow$  **removing axioms** from  $\mathcal{D}$ .

Instead, we want to **weaken axioms** in  $\mathcal{H} \Rightarrow$  **Gentle Repair!**

Given axioms  $\beta, \gamma$ , an axiom  $\gamma$  is **weaker than**  $\beta$  if  $Con(\{\gamma\}) \subset Con(\{\beta\})$

## Illustration

## Illustration

$$\mathcal{D}_s := \{\exists \text{receives.}(Gift \sqcap Deluxe) \sqsubseteq \exists \text{gets.}Bribe\}$$

$$\mathcal{D}_r := \{IndonesianPolitician \sqsubseteq \exists \text{receives.}(Gift \sqcap Deluxe)\}$$

- Every Indonesian politician is bribed w.r.t.  $\mathcal{D}_s \cup \mathcal{D}_r$ .



## Illustration

$$\mathcal{D}_s := \{ \exists \text{receives.} (Gift \sqcap Deluxe) \sqsubseteq \exists \text{gets.} Bribe \}$$

$$\mathcal{D}_r := \{ IndonesianPolitician \sqsubseteq \exists \text{receives.} (Gift \sqcap Deluxe) \}$$

- Every Indonesian politician is bribed w.r.t.  $\mathcal{D}_s \cup \mathcal{D}_r$ .
- **Classical:** Removes a “common knowledge”:  
 $IndonesianPolitician \sqsubseteq \exists \text{receives.} (Gift \sqcap Deluxe)$





## Illustration

$$\mathcal{D}_s := \{\exists \text{receives.}(Gift \sqcap Deluxe) \sqsubseteq \exists \text{gets.}Bribe\}$$

$$\mathcal{D}_r := \{IndonesianPolitician \sqsubseteq \exists \text{receives.}(Gift \sqcap Deluxe)\}$$

- Every Indonesian politician is bribed w.r.t.  $\mathcal{D}_s \cup \mathcal{D}_r$ .
- **Classical:** Removes a “common knowledge”:  
 $IndonesianPolitician \sqsubseteq \exists \text{receives.}(Gift \sqcap Deluxe)$
- **Gentle:** Weaken  $\beta \in \mathcal{D}_r$  to  $IndonesianPolitician \sqsubseteq \exists \text{receives.}Gift$   
But, this consequence  $IndonesianPolitician \sqsubseteq \exists \text{receives.}Deluxe$  is also gone.



## Illustration

$$\mathfrak{D}_s := \{ \exists \text{receives.} (Gift \sqcap Deluxe) \sqsubseteq \exists \text{gets.} Bribe \}$$

$$\mathfrak{D}_r := \{ IndonesianPolitician \sqsubseteq \exists \text{receives.} (Gift \sqcap Deluxe) \}$$

- Every Indonesian politician is bribed w.r.t.  $\mathfrak{D}_s \cup \mathfrak{D}_r$ .
- **Classical:** Removes a “common knowledge”:  
 $IndonesianPolitician \sqsubseteq \exists \text{receives.} (Gift \sqcap Deluxe)$
- **Gentle:** Weaken  $\beta \in \mathfrak{D}_r$  to  $IndonesianPolitician \sqsubseteq \exists \text{receives.} Gift$   
But, this consequence  $IndonesianPolitician \sqsubseteq \exists \text{receives.} Deluxe$  is also gone.
- **More gentle:** Weaken  $\beta$  to  
 $IndonesianPolitician \sqsubseteq \exists \text{receives.} Gift \sqcap \exists \text{receives.} Deluxe$



# How to Make it Gentle?

## Gentle Repair Algorithm: [BaKrNuPe, KR 2018]

- Take all justifications and one minimal hitting set  $\mathcal{H}_{min}$
- For each  $\beta \in \mathcal{H}_{min}$  and all  $J_1, \dots, J_k$  containing  $\beta$ ,  
replace  $\beta$  with **exactly one**  $\gamma$ , where  $\gamma$  is weaker than  $\beta$  such that

$$\mathcal{D}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \text{ for } i = 1, \dots, k. \quad (1)$$

$\gamma$  always exists.

- **Construct**  $\mathcal{D}'$  **obtained** from  $\mathcal{D}_r$  by **replacing** each  $\beta \in \mathcal{H}_{min}$  with an appropriate weaker  $\gamma$  satisfying (1).
- **Check** if  $\alpha$  is a consequence of  $\mathcal{D}_s \cup \mathcal{D}'$ .

# How to Make it Gentle?

## Gentle Repair Algorithm: [BaKrNuPe, KR 2018]

- Take all justifications and one minimal hitting set  $\mathcal{H}_{min}$
- For each  $\beta \in \mathcal{H}_{min}$  and all  $J_1, \dots, J_k$  containing  $\beta$ ,  
replace  $\beta$  with **exactly one**  $\gamma$ , where  $\gamma$  is weaker than  $\beta$  such that

$$\mathcal{D}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \text{ for } i = 1, \dots, k. \quad (1)$$

$\gamma$  always exists.

- **Construct**  $\mathcal{D}'$  **obtained** from  $\mathcal{D}_r$  by **replacing** each  $\beta \in \mathcal{H}_{min}$  with an appropriate weaker  $\gamma$  satisfying (1).
- **Check** if  $\alpha$  is a consequence of  $\mathcal{D}_s \cup \mathcal{D}'$ .

## Obtaining Gentle Repairs needs Iterations

- Using the algorithm above,  $\alpha$  still can be a consequence of  $\mathcal{D}_s \cup \mathcal{D}'$ .
- Solution: Just **iterate** Gentle Repair Algorithm until  $\mathcal{D}_s \cup \mathcal{D}' \not\models \alpha$ .
- The iterative algorithm yields **an exponential upper bound** on the number of iterations.

# Weakening Relations

To obtain better bounds on the number of iterations, introduce weakening relations on axioms.

## Weakening Relation

# Weakening Relations

To obtain better bounds on the number of iterations, introduce weakening relations on axioms.

## Weakening Relation

The binary relation  $\succ$  on axioms is

- a **weakening relation** if  $\beta \succ \gamma$  implies that  $\gamma$  is weaker than  $\beta$ ;
- **well-founded** if there is no infinite  $\succ$ -chain  $\beta_1 \succ \beta_2 \succ \beta_3 \succ \dots$ ;
- **complete** if for any  $\beta$  that is not a tautology, there is a tautology  $\gamma$  s.t.  $\beta \succ \gamma$ .
- **linear (polynomial)** if for every axiom  $\beta$ , the length of the longest chain  $\succ$ -generated from  $\beta$  is **linearly (polynomially)** bounded by the size of  $\beta$ ;

# Weakening Relations

## Weakening Relation

The binary relation  $\succ$  on axioms is

- a **weakening relation** if  $\beta \succ \gamma$  implies that  $\gamma$  is weaker than  $\beta$ ;
- **well-founded** if there is no infinite  $\succ$ -chain  $\beta_1 \succ \beta_2 \succ \beta_3 \succ \dots$ ;
- **complete** if for any  $\beta$  that is not a tautology, there is a tautology  $\gamma$  s.t.  $\beta \succ \gamma$ .
- **linear (polynomial)** if for every axiom  $\beta$ , the length of the longest chain  $\succ$ -generated from  $\beta$  is **linearly (polynomially)** bounded by the size of  $\beta$ ;



Weakening relations making **larger steps** may **decrease** the number of iterations



Weakening relations making **smaller steps** may make the repair more gentle

# Maximally Strong Weakening Axioms

Replace  $\beta$  with exactly one weaker  $\gamma$  s.t.

$$\mathfrak{D}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \text{ for } i = 1, \dots, k$$

If  $\gamma$  is a tautology, then it is the same as classical repair.

To make this repair as gentle as possible,  $\gamma$  should be **maximally strong**

$$\begin{array}{l} \mathfrak{D}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \\ \text{but for all } \delta \text{ such that } \beta \succ \delta \succ \gamma, \text{ we have} \\ \mathfrak{D}_s \cup (J_i \setminus \{\beta\}) \cup \{\delta\} \models \alpha \end{array}$$



# Maximally Strong Weakening Axioms

Replace  $\beta$  with exactly one weaker  $\gamma$  s.t.

$$\mathfrak{S}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \text{ for } i = 1, \dots, k$$

If  $\gamma$  is a tautology, then it is the same as classical repair.

To make this repair as gentle as possible,  $\gamma$  should be **maximally strong**

$$\begin{array}{l} \mathfrak{S}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \\ \text{but for all } \delta \text{ such that } \beta \succ \delta \succ \gamma, \text{ we have} \\ \mathfrak{S}_s \cup (J_i \setminus \{\beta\}) \cup \{\delta\} \models \alpha \end{array}$$

Do they always  
exist?

How to compute  
them?

# Weakening Relations in $\mathcal{EL}$

Focus on GCIs and generalize the right-hand side of GCIs.

A Weakening Relation  $\succ^{sub}$

$C \sqsubseteq D \succ^{sub} C' \sqsubseteq D'$  if  $C' = C$ ,  $D \sqsubseteq D'$ , and  
 $\{C' \sqsubseteq D'\} \not\equiv C \sqsubseteq D$ .

$D \sqsubseteq^{syn} D' \Rightarrow$  removing occurrences of subconcepts of  $D$ .

A Weakening Relation  $\succ^{syn}$

$C \sqsubseteq D \succ^{syn} C' \sqsubseteq D'$  if  $C' = C$  and  $D \sqsubseteq^{syn} D'$ , and  
 $\{C' \sqsubseteq D'\} \not\equiv C \sqsubseteq D$ .

# Weakening Relations in $\mathcal{EL}$

Focus on GCIs and generalize the right-hand side of GCIs.

A Weakening Relation  $\succ^{sub}$

$C \sqsubseteq D \succ^{sub} C' \sqsubseteq D'$  if  $C' = C$ ,  $D \sqsubseteq D'$ , and  
 $\{C' \sqsubseteq D'\} \not\equiv C \sqsubseteq D$ .

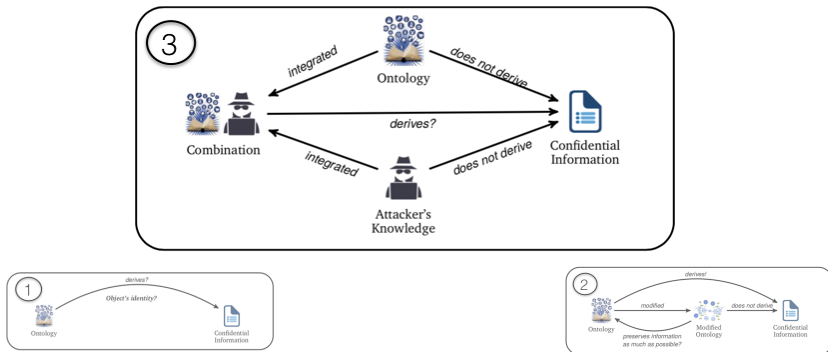
Employing both, maximally strong weakenings can be effectively computed

$D \sqsubseteq^{syn} D' \Rightarrow$  removing occurrences of subconcepts of  $D$ .

A Weakening Relation  $\succ^{syn}$

$C \sqsubseteq D \succ^{syn} C' \sqsubseteq D'$  if  $C' = C$  and  $D \sqsubseteq^{syn} D'$ , and  
 $\{C' \sqsubseteq D'\} \not\equiv C \sqsubseteq D$ .

# Problem 3: Privacy-Preserving Ontology Publishing (PPOP)



## PPOP for $\mathcal{EL}$ Ontologies ([DL 2018], [JELIA 2019], [KI 2019])

Restricting the ontology:

- $\mathcal{EL}$  Instance Stores &  $\mathcal{EL}$  ABoxes (**No TBoxes**)
- **Instance Stores:** Ontologies without individual relationships

# PPOP for $\mathcal{EL}$ Instance Stores



$\mathcal{EL}$  Instance Stores  
without TBox



$C_1(a), C_2(a)$  implies  $(C_1 \sqcap C_2)(a)$

only one concept assertion  
speaking about one individual



Published  
Information  
(an  $\mathcal{EL}$  Concept  $C$ )



Attacker's  
Knowledge  
(an  $\mathcal{EL}$  /  $\mathcal{FL}_0$  /  $\mathcal{FLE}$   
Concept  $E$ )



Confidential Information  
(a **finite set of**  
 $\mathcal{EL}$  **concepts**)  
 $\{D_1, \dots, D_p\}$

**Confidential Information**  $\mathcal{P} = \{D\}$  about *LINDA*



$D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$

Original **Published Information**  $C$  about *LINDA*



$C = Patient \sqcap Female$   
 $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C$  is not **compliant with**  $D$

**Confidential Information**  $\mathcal{P} = \{D\}$  about *LINDA*



$D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$

Original **Published Information**  $C$  about *LINDA*



$C = Patient \sqcap Female$   
 $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C$  is not **compliant with**  $D$

**Modification**



$C_1 = Female \sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C \sqsubseteq C_1$  and  $C_1$  **complies with**  $D$

# Privacy Attacks in $\mathcal{EL}$ Instance Stores

**Confidential Information**  $\mathcal{P} = \{D\}$  about *LINDA*



$D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$

Original **Published Information**  $C$  about *LINDA*



$C = Patient \sqcap Female$

$\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C$  is not **compliant with**  $D$

**$\mathcal{EL}$ -Attacker is Coming!**



$C_1 = Female \sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$



He knows  $Patient(LINDA)$



**Confidential Information**  $\mathcal{P} = \{D\}$  about *LINDA*



$D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$

Original **Published Information**  $C$  about *LINDA*



$C = Patient \sqcap Female$   
 $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C$  is not **compliant with**  $D$

**Linked and Revealed!**



$C'_1 = Female \sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$   
 $\sqcap$  **Patient**

Note  $D(LINDA)$  is **revealed** and  $C_1$  is not  $\mathcal{EL}$ -safe for  $D$

**Confidential Information**  $\mathcal{P} = \{D\}$  about *LINDA*



$D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$

Original **Published Information**  $C$  about *LINDA*



$C = Patient \sqcap Female$   
 $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C$  is not **compliant with**  $D$

**Modification**



$C_2 = Female \sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.T)$   
 $\sqcap \exists seenBy.(Male \sqcap worksIn.Oncology)$

$C_2$  is  $\mathcal{EL}$ -safe for  $D$

**Confidential Information**  $\mathcal{P} = \{D\}$  about *LINDA*



$D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$

Original **Published Information**  $C$  about *LINDA*



$C = Patient \sqcap Female$   
 $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C$  is not **compliant with**  $D$

**$\mathcal{FL}_0$ -Attacker is Coming!**



$C_2 = Female \sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.T)$   
 $\sqcap \exists seenBy.(Male \sqcap worksIn.Oncology)$



He knows  $(Patient \sqcap \forall seenBy.\forall worksIn.Oncology)(LINDA)$

**Confidential Information**  $\mathcal{P} = \{D\}$  about *LINDA*



$D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$

Original **Published Information**  $C$  about *LINDA*



$C = Patient \sqcap Female$

$\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C$  is not **compliant with**  $D$

**Linked and Revealed!**



$C'_2 = Female \sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.T)$

$\sqcap \exists seenBy.(Male \sqcap worksIn.Oncology)$

$\sqcap$   **$Patient \sqcap \forall seenBy.\forall worksIn.Oncology$**

$D(LINDA)$  is revealed again and  $C_2$  is not  $\mathcal{FL}_0$ -safe for  $D$

**Confidential Information**  $\mathcal{P} = \{D\}$  about *LINDA*



$D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$

Original **Published Information**  $C$  about *LINDA*



$C = Patient \sqcap Female$   
 $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$

Note  $C$  is not **compliant with**  $D$

**Modification**



$C_3 = Female \sqcap Patient \sqcap \exists seenBy.(Doctor \sqcap Male)$

$C_3$  is  $\mathcal{FL}_0$ -safe for  $D$

# Decision & Computational Problems for Instance Stores

Given  $\mathcal{L} \in \{\mathcal{EL}, \mathcal{FL}_0, \mathcal{FLE}\}$ , a published information ( $\mathcal{EL}$  concept)  $C$ , an  $\mathcal{EL}$  confidential information  $\mathcal{P}$ .

## Decision Problems

- **Compliance:**  
*Is an  $\mathcal{EL}$  concept  $C$  compliant with  $\mathcal{P}$ ?*
- **$\mathcal{L}$ -Safety:**  
*Is an  $\mathcal{EL}$  concept  $C$   $\mathcal{L}$ -safe for  $\mathcal{P}$ ?*
- **OptCom:**  
*Is an  $\mathcal{EL}$  concept  $C_1$  an optimal compliant generalization of  $C$  w.r.t.  $\mathcal{P}$ ?*
- **$\mathcal{L}$ -Optimality:**  
*Is an  $\mathcal{EL}$  concept  $C_1$  an optimal  $\mathcal{L}$ -safe generalization of  $C$  for  $\mathcal{P}$ ?*

## Note

Optimal: For all  $C_2$ , if  $C_2 \sqsubset C_1$ , then  $C_2$  is not (compliant)  $\mathcal{L}$ -safe w.r.t.  $\mathcal{P}$ .

# Decision & Computational Problems for Instance Stores

Given  $\mathcal{L} \in \{\mathcal{EL}, \mathcal{FL}_0, \mathcal{FLE}\}$ , a published information ( $\mathcal{EL}$  concept)  $C$ , an  $\mathcal{EL}$  confidential information  $\mathcal{P}$ .

## Decision Problems

- **Compliance:**  
*Is an  $\mathcal{EL}$  concept  $C$  compliant with  $\mathcal{P}$ ?*
- **$\mathcal{L}$ -Safety:**  
*Is an  $\mathcal{EL}$  concept  $C$   $\mathcal{L}$ -safe for  $\mathcal{P}$ ?*
- **OptCom:**  
*Is an  $\mathcal{EL}$  concept  $C_1$  an optimal compliant generalization of  $C$  w.r.t.  $\mathcal{P}$ ?*
- **$\mathcal{L}$ -Optimality:**  
*Is an  $\mathcal{EL}$  concept  $C_1$  an optimal  $\mathcal{L}$ -safe generalization of  $C$  for  $\mathcal{P}$ ?*

## Computational Problem

*Find an  $\mathcal{EL}$  concept  $C_1$  s.t  $C_1$  is an optimal (compliant)  $\mathcal{L}$ -safe generalization of  $C$  for  $\mathcal{P}$ !*

# Complexity Results on PPOP for $\mathcal{EL}$ Instance Stores

Compliance is in PTime, whereas OptCom is in coNP, but Dual-hard.

<b>Decision Problems</b>	$\mathcal{L} = \mathcal{EL}$	$\mathcal{L} = \mathcal{FL}_0$	$\mathcal{L} = \mathcal{FLE}$
$\mathcal{L}$ -safety	PTime	PTime	PTime
$\mathcal{L}$ -optimality	coNP and Dual-hard	coNP and Dual-hard	PTime

Table: Complexity results of  $\mathcal{L}$ -safety and  $\mathcal{L}$ -optimality on PPOP for  $\mathcal{EL}$  instance stores

Optimal Compliance Generalization(s) can be computed in ExpTime.

<b>Computational Problems</b>	$\mathcal{L} = \mathcal{EL}$	$\mathcal{L} = \mathcal{FL}_0$	$\mathcal{L} = \mathcal{FLE}$
Optimal $\mathcal{L}$ -safe Generalization(s)	ExpTime	ExpTime	PTime

Table: Complexity of computing one/all optimal  $Q$ -safe generalizations for  $\mathcal{P}$



Including relationships between individuals in  $\mathcal{EL}$  ABoxes.



Published  
Information  
(an  $\mathcal{EL}$  ABox)



Attacker's  
Knowledge  
(an  $\mathcal{EL}$  ABox)



Confidential Information  
(an  $\mathcal{EL}$  concept or  
a conjunctive query)

Including relationships between individuals in  $\mathcal{EL}$  ABoxes.



Published  
Information  
(an  $\mathcal{EL}$  ABox)



Attacker's  
Knowledge  
(an  $\mathcal{EL}$  ABox)

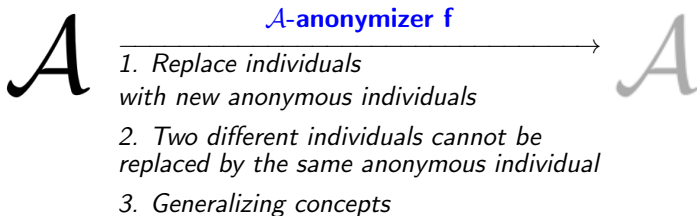


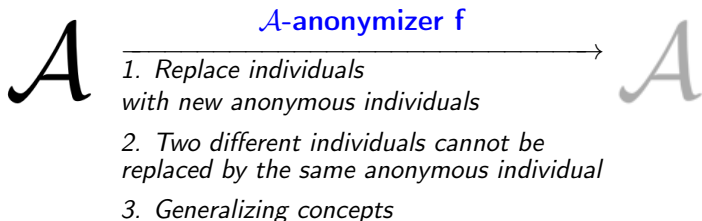
Confidential Information  
(an  $\mathcal{EL}$  concept or  
a conjunctive query)

Given an  $\mathcal{EL}$  ABox  $\mathcal{A}$ , and a confidential information  $\mathcal{P}$  that is either an **instance query** ( $\mathcal{EL}$  concept)  $D$  or a **conjunctive query**  $q$ .

- $\mathcal{A}$  is **compliant** with  $D$  iff  $\mathcal{A} \not\models D(a)$  for all individuals  $a$ .
- $\mathcal{A}$  is **compliant** with  $q$  iff  $\mathcal{A} \not\models q(\vec{a})$  for all tuples  $\vec{a}$  of individuals.
- $\mathcal{A}$  is **safe** for  $\mathcal{P}$  iff for all (attackers' knowledge)  $\mathcal{A}'$  complying with  $\mathcal{P}$ ,  $\mathcal{A} \cup \mathcal{A}'$  complies with  $\mathcal{P}$

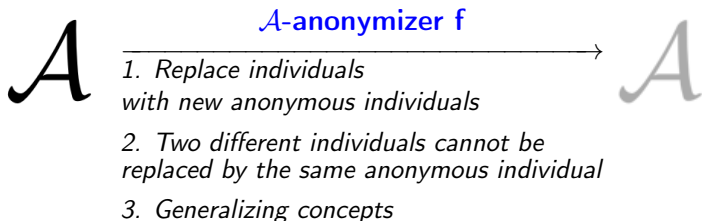
How to modify  $\mathcal{EL}$  ABoxes?





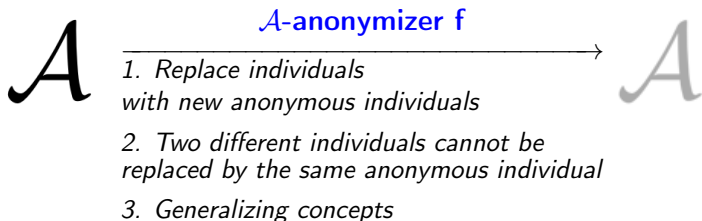
## ABox Anonymization

$$\mathcal{A}_0 := \{ \text{Doctor} \sqcap \exists \text{worksIn.Oncology}(\text{LINDA}), \\ \text{seenBy}(\text{BOB}, \text{LINDA}) \}$$
$$\downarrow f_1 \checkmark$$
$$\mathcal{A}_1 := \{ \text{Doctor} \sqcap \exists \text{worksIn.Oncology}(y), \\ \text{seenBy}(x, \text{LINDA}) \}$$



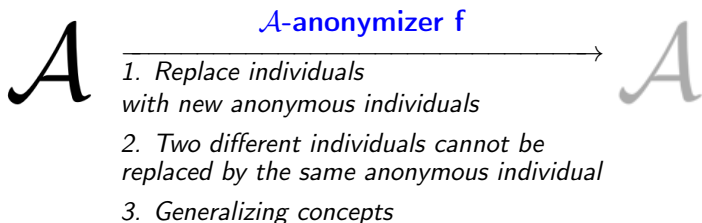
## ABox Anonymization

$$\mathcal{A}_0 := \{ \text{Doctor} \sqcap \exists \text{worksIn.Oncology}(\text{LINDA}), \\ \text{seenBy}(\text{BOB}, \text{LINDA}) \}$$
$$\downarrow f_2 \quad \times$$
$$\mathcal{A}_2 := \{ \text{Doctor} \sqcap \exists \text{worksIn.Oncology}(z), \\ \text{seenBy}(z, \text{LINDA}) \}$$



## ABox Anonymization

$$\mathcal{A}_0 := \{ \text{Doctor} \sqcap \exists \text{worksIn.Oncology}(\text{LINDA}), \\ \text{seenBy}(\text{BOB}, \text{LINDA}) \}$$
$$\downarrow f_3 \checkmark$$
$$\mathcal{A}_3 := \{ \text{Doctor} \sqcap \exists \text{worksIn}.\top(y), \\ \text{seenBy}(\text{BOB}, \text{LINDA}) \}$$



## Measuring Optimality

An  $\mathcal{A}$ -anonymizer  $f_2$  is **more informative than** an  $\mathcal{A}$ -anonymizer  $f_1$  ( $f_2 > f_1$ ) if  $f_2$  can be obtained from  $f_1$  by:

- keeping more known individuals
- identifying more distinct anonymous individuals
- specializing more  $\mathcal{E}\mathcal{L}$  concepts

# Decision Problems on PPOP for $\mathcal{EL}$ ABoxes

Given an  $\mathcal{EL}$  ABox  $\mathcal{A}$ , an  $\mathcal{EL}$  concept  $D$ , and an  $\mathcal{A}$ -anonymizer  $f$ ,

- **Compliance** <sub>$IQ$</sub> , **Safety** <sub>$IQ$</sub> , and
- **Optimal-Compliance** <sub>$IQ$</sub>  (**Optimal-Safety** <sub>$IQ$</sub> ) asks
  - if  $f(\mathcal{A})$  is compliant with (safe for)  $D$  and
  - for all  $\mathcal{A}$ -anonymizers  $f'$ , if  $f' > f$ , then  $f'(\mathcal{A})$  is not compliant with (safe for)  $D$

Analogous for **Compliance** <sub>$CQ$</sub> , **Safety** <sub>$CQ$</sub> , **Optimal-Compliance** <sub>$CQ$</sub> , and **Optimal-Safety** <sub>$CQ$</sub> , where the policy is a CQ



# Decision Problems on PPOP for $\mathcal{EL}$ ABoxes

Given an  $\mathcal{EL}$  ABox  $\mathcal{A}$ , an  $\mathcal{EL}$  concept  $D$ , and an  $\mathcal{A}$ -anonymizer  $f$ ,

- **Compliance** <sub>$\text{IQ}$</sub> , **Safety** <sub>$\text{IQ}$</sub> , and
- **Optimal-Compliance** <sub>$\text{IQ}$</sub>  (**Optimal-Safety** <sub>$\text{IQ}$</sub> ) asks
  - if  $f(\mathcal{A})$  is compliant with (safe for)  $D$  and
  - for all  $\mathcal{A}$ -anonymizers  $f'$ , if  $f' > f$ , then  $f'(\mathcal{A})$  is not compliant with (safe for)  $D$

Analogous for **Compliance** <sub>$\text{CQ}$</sub> , **Safety** <sub>$\text{CQ}$</sub> , **Optimal-Compliance** <sub>$\text{CQ}$</sub> , and **Optimal-Safety** <sub>$\text{CQ}$</sub> , where the policy is a CQ

Decision Problems	$X = \text{IQ}$	$X = \text{CQ}$
Compliance <sub><math>X</math></sub>	PTime	coNP-complete
Safety <sub><math>X</math></sub>	PTime	$\Pi_2^P$ and DP-hard
Optimal-Compliance <sub><math>X</math></sub>	coNP and Dual-hard	$\Pi_2^P$ and DP-hard
Optimal-Safety <sub><math>X</math></sub>	coNP and Dual-hard	$\Pi_3^P$ and DP-hard

Table: Complexity Results on PPOP in  $\mathcal{EL}$  ABoxes

# Conclusions

## *The Identity Problem:*

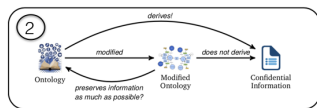
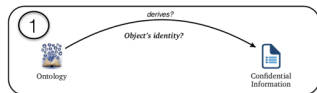
- Non trivial for DLs with equality power
- Introducing variants of the identity problem
- Reduction to classical reasoning in DLs

## *Gentle Repair:*

- Introducing a framework for repair via axiom weakening
- Weakening relations
- Weakening axioms in  $\mathcal{EL}$

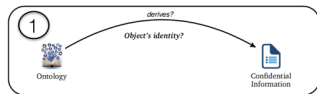
## *Privacy-Preserving Ontology Publishing:*

- PPOP for  $\mathcal{EL}$  Instance Stores
- PPOP for  $\mathcal{EL}$  ABoxes
- Applying the concepts of compliance, safety, and optimality in both settings



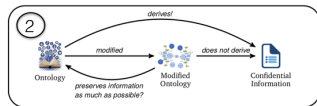
## *The Identity Problem:*

- Formalizing the “real” definition of  $k$ -Anonymity
- Adding probability to the setting



## *Gentle Repair:*

- Choosing which axioms to be repaired
- Which maximally strong weakening is the best?
- Weakening relations for other DLs



## *Privacy-Preserving Ontology Publishing:*

- Computing the optimal compliant (safe) anonymization
- Finding a more gentle weakening relation for ABox anonymization
- Including TBox/attackers' meta knowledge? (Bonatti et. al., 2013)



- Franz Baader, Daniel Borchmann, and **Adrian Nuradiansyah**, *Preliminary Results on the Identity Problem in Description Logic Ontologies*, DL 2017, Montpellier, 2017.
- Franz Baader, Daniel Borchmann, and **Adrian Nuradiansyah**, *The Identity Problem in Description Logic Ontologies and Its Applications to View-Based Information Hiding*, JIST 2017, Gold Coast, 2017.
- Franz Baader, Francesco Kriegel, **Adrian Nuradiansyah**, and Rafael Peñaloza, *Making Repairs in Description Logics More Gentle*, KR 2018, Tempe, 2018.
- Franz Baader and **Adrian Nuradiansyah**, *Towards Privacy-Preserving Ontology Publishing*, DL 2018, Tempe, 2018.
- Franz Baader, Francesco Kriegel, and **Adrian Nuradiansyah**, *Privacy-Preserving Ontology Publishing for  $\mathcal{EL}$  Instance Stores*, JELIA 2019, Rende, 2019.
- Franz Baader and **Adrian Nuradiansyah**, *Mixing Description Logics in Privacy-Preserving Ontology Publishing*, KI 2019, Kassel, 2019.

## Research Visits:

- Visiting Prof. **Rafael Peñaloza** at Free University of Bozen-Bolzano, March 1-May 16, 2018.
- Visiting Prof. **Bernardo Cuenca Grau** at the University of Oxford, UK, April 1 - June 30, 2019.

## Awards:

- **The Best Student Paper Award** at the 7th Joint International Semantic Technology Conference (JIST 2017) at Gold Coast, Australia.
- Shortlisted for **The Best Paper Award** at the Künstliche Intelligenz Conference (KI 2019) at Kassel, Germany.

# Thank You

