

Example for the definition of a lift

Program SUM:

1. $\text{sum}(x, 0, x) \leftarrow,$
2. $\text{sum}(x, s(y), s(z)) \leftarrow \text{sum}(x, y, z),$

An SLD-derivation ξ :

$$\begin{aligned}\text{sum}(s(s(0)), s(s(0)), z) &\Rightarrow_2 \text{sum}(s(s(0)), s(0), z_1) \Rightarrow_2 \\ \text{sum}(s(s(0)), 0, z_2) &\Rightarrow_1 []\end{aligned}$$

An SLD-derivation ξ' :

$$\text{sum}(x', y', z') \Rightarrow_2 \text{sum}(x'_1, y'_1, z'_1) \Rightarrow_2 \text{sum}(x'_2, y'_2, z'_2) \Rightarrow_1 []$$

An SLD-derivation ξ'' :

$$\begin{aligned}\text{sum}(x', y', z') &\Rightarrow_2 \text{sum}(x'_1, y'_1, z'_1) \Rightarrow_2 \text{sum}(x'_2, y'_2, z'_2) \Rightarrow_2 \\ \text{sum}(x'_3, y'_3, z'_3) &\dots\end{aligned}$$